

Speculative Betas

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Introduction

Model

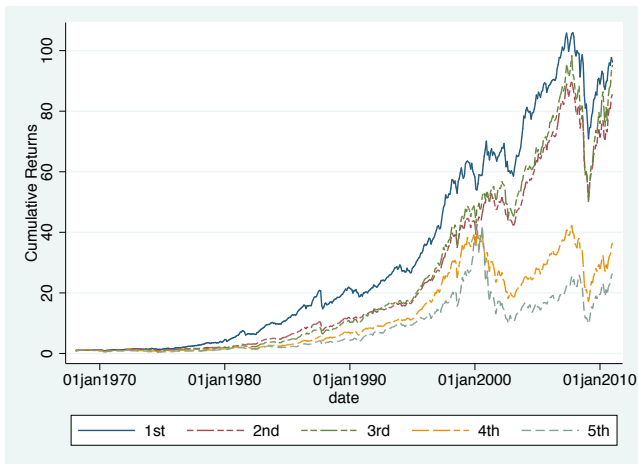
1 factor static

Shorting

OLG Exension

Calibration

High Risk, Low Return Puzzle



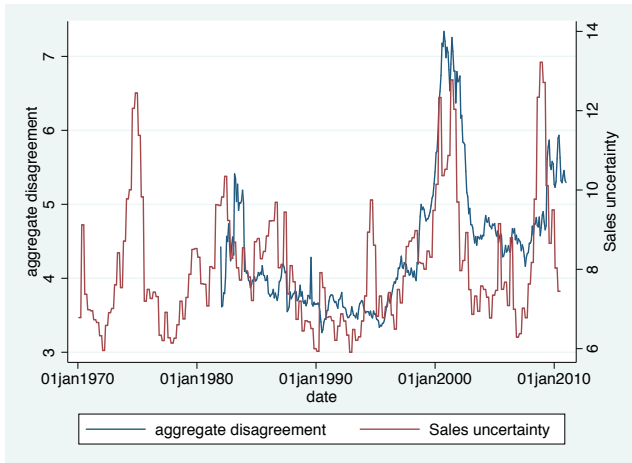
- ▶ Beta-neutral strategy of long low beta / short high beta stocks has Sharpe of 0.75 (BBW ('11))
- ▶ Black ('72), Pratt ('67), Friend and Blume ('70)

Our Explanation

Disagreement about **aggregate** cash-flows + short-sales constraints

- ▶ Non-private information, agree to disagree
- ▶ Evidence of disagreement among professional forecasters and households
 - ▶ On macroeconomic state variables such as market earnings, industrial production growth and inflation (Cukierman and Wachtel '79, Zarnowitz and Lambros '87, Kandel and Pearson '95, Mankiw, Romer and Wolfers '04)
 - ▶ Dispersion in professional forecasts about stock market earnings varies over time and is correlated with aggregate economic uncertainty indicators (Bloom '09, Lamont '02, Yu '10)
 - ▶ Disagreement due to heterogeneous priors or cognitive biases such as overconfidence that result in agents over-weighting private signals

Bloom (2012) uncertainty measure and modified Yu (2012) analyst forecast dispersion measure



Short-Selling Constraints

- ▶ Short-selling costly due to institutional constraints
- ▶ Large fraction of mutual funds, 20 trillion dollars under management, can't short by charter and can't use derivatives (Almazan et al. '04, Koski and Pontiff '99)
- ▶ Hedge fund sector with 1.8 trillion dollars can and do short

Key Features of Model

- ▶ Otherwise CAPM framework: cashflows of firms follow a one factor model
- ▶ Disagree about the mean of common factor and not variances
- ▶ Buyers such as retail mutual funds
- ▶ Arbitrageurs such as hedge funds who short
- ▶ Multi-asset model based on Chen, Hong and Stein 01's rendition of Miller '77 single stock economy
 - ▶ Divergence of opinion leads to over-pricing because price reflects only the views of the optimists

The Main Idea

- ▶ β scales aggregate disagreement

$$\tilde{d}^i = \beta^i \tilde{z} + \tilde{\epsilon}^i$$

1. **High β assets are more sensitive to disagreement about aggregate cashflows** than low β assets.
2. Macro-disagreement: optimists $\bar{z} + \lambda$, pessimists $\bar{z} - \lambda$
3. High β experience **more divergence of opinion**: optimist $\beta^i(\bar{z} + \lambda)$ and pessimists $\beta^i(\bar{z} - \lambda)$
4. Then **over-pricing** due to short-sales constraints
5. More shorting from arbs on high β

⇒ CAPM holds when aggregate disagreement is low

⇒ But high disagreement leads to inverted-U shaped: initially increasing with beta and then decreasing

- ▶ Kinked/concave/inverted-U shaped relationship due to disagreement having to be large enough to over-come benefits of diversification (cost of bearing idiosyncratic risk)

OLG Extension

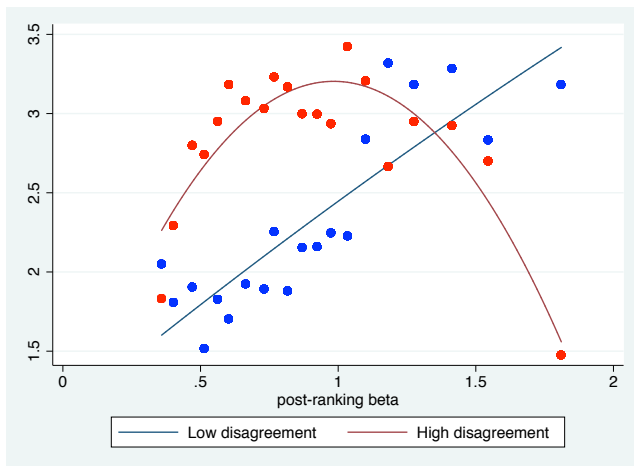
- ▶ OLG extension to show results go through + additional implication that high *beta* stocks have higher share turnover
- ▶ Calibration exercise

Empirics

- ▶ Use modified Yu (2010) measure of dispersion of earnings forecasts and cross-sectional SD of sales growth Bloom '09
- ▶ Test basic predictions/premises of the model:
 1. Upward sloping SML when disagreement/uncertainty is low.
 2. Inverted U-shape of SML when disagreement is high
 3. More **stock-level disagreement on high β stocks**, especially when high aggregate disagreement.
 4. More **shorting on high β stocks**, especially when high aggregate disagreement.
 5. More **turnover on high β stocks**, especially when high aggregate disagreement.

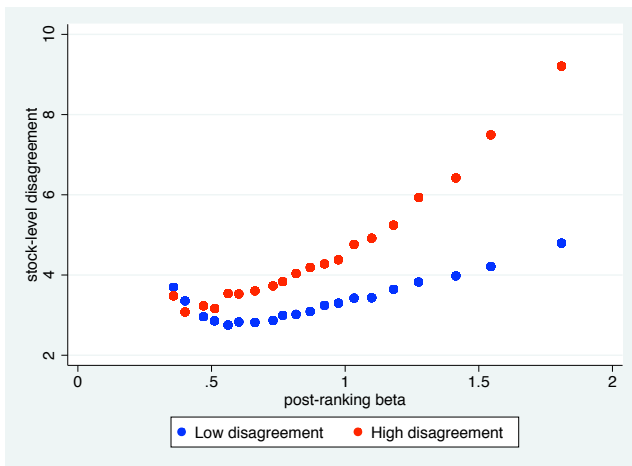
Disagreement and CAPM: kinks

Figure: Average 3-months excess returns for equal-weighted beta decile portfolios in low and high aggregate disagreement months.



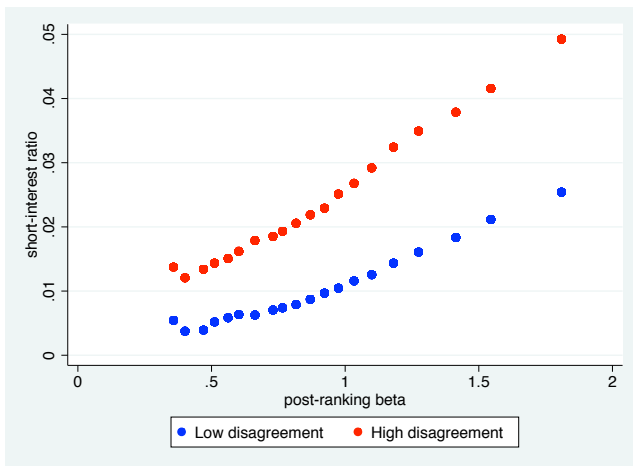
Stock-level disagreement, β and aggregate disagreement.

Figure: Equal-weighted average of dispersion of analyst earnings forecasts by beta deciles during low and high aggregate disagreement months.



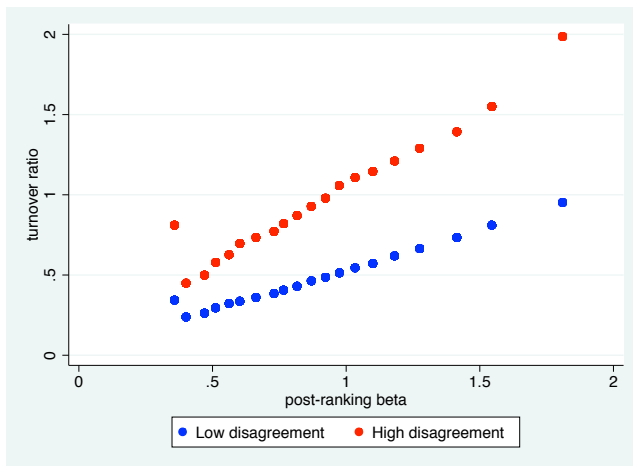
Disagreement, β and shorting activity

Figure: Equal-weighted average of short interest ratio by beta deciles during low and high aggregate disagreement months.



Disagreement and share turnover

Figure: Equal-weighted average of share turnover for stocks by beta deciles during low and high aggregate disagreement months.



Outline

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Model

- ▶ Dates $t = 0, 1$
- ▶ N risky assets and **exogenous** risk-free rate is r
- ▶ Risky asset i delivers a dividend \tilde{d}_i at date 1:

$$\forall i \in \{1, \dots, N\}, \quad \tilde{d}_i = b_i \tilde{z} + \tilde{\epsilon}_i,$$

where $\tilde{z} \sim \mathcal{N}(\bar{z}, \sigma_z^2)$, $\tilde{\epsilon}_i \sim \mathcal{N}(0, \sigma_\epsilon^2)$, and $\text{cov}(\tilde{z}, \tilde{\epsilon}_i) = 0$

- ▶ Each asset is in supply $\frac{1}{N}$:

$$0 < b_1 < b_2 < \dots < b_N$$

- ▶ Assume $\sum_{i=1}^N \frac{b_i}{N} = 1$.

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- ▶ Assume $\sum_{i=1}^N \frac{b_i}{N} = 1$.

Investors' Preferences and Beliefs

- ▶ Two groups of investors:
 - ▶ Short-sales constrained with heterogenous beliefs (MF - fraction α)
 - ▶ Unconstrained with homogenous beliefs (HF or arbs - fraction $1 - \alpha$)
- ▶ Investors have mean-variance utility functions with variance weight $\frac{1}{2\gamma}$ (or CARA with risk tolerance γ)
- ▶ Heterogeneous beliefs about aggregate factor:

$$\mathbb{E}^A[\tilde{z}] = \bar{z} + \lambda \quad \text{and} \quad \mathbb{E}^B[\tilde{z}] = \bar{z} - \lambda \quad \text{with} \quad \lambda > 0$$

- ▶ Proportion $\frac{1}{2}$ of optimists/pessimists among SSC agents.
- ▶ Investors hold correct expectations about the variance of \tilde{z} .

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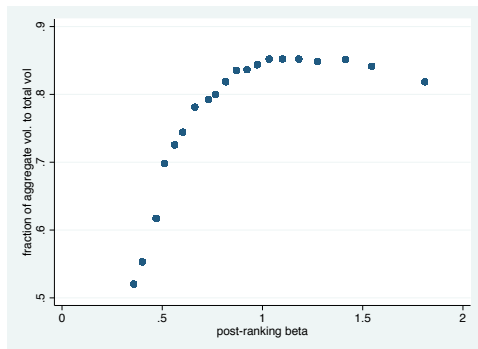
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Homoskedasticity

- ▶ This is just to simplify the exposition.
- ▶ If dividends are heteroskedastic, then need to re-rank assets according to: $\frac{b_1}{\sigma_1^2} < \dots < \frac{b_N}{\sigma_N^2}$
- ▶ In the data, $\frac{b_i}{\sigma_i^2}$ is highly correlated with b_i :

Figure: Sample: CRSP. Period: 1982-2010.



Discussion of other assumptions

1. Can also have disagreement about idiosyncratic but too easy
2. No disagreement on variance/covariance matrix.
 - ▶ Jarrow '80: more general structure but less clear implications than 1-factor model
3. Strict short-selling constraints. (realistic – MF)
 - ▶ Works with any strictly convex cost function.

Solving for the equilibrium

- ▶ Intuition: investors **disagree on expected payoffs**.
 - ▶ Mechanically, disagreement is higher for high b assets ($\mathbb{E}^i[\tilde{d}] = b^i \mathbb{E}^i[\tilde{z}]$).
 - ▶ Pessimists hit binding short-sales constraints on **high b assets first**.
1. Posit equilibrium structure: $\bar{j} \in [1, N]$ such that:
 - ▶ Assets $i \geq \bar{j}$ (i.e. $b_i > b_j$) such that pessimists are sidelined.
 - ▶ All investors are long assets $i < \bar{j}$.
 2. Derive equilibrium pricing equations under \bar{j} .
 3. Write down conditions under which \bar{j} is the marginal asset.

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Maximization program

- ▶ Agents are maximizing:

$$\max_{\mu_i^k} \sum_{i=1}^N \mu_i^k (b_i \mathbb{E}^k[\tilde{z}] - (1+r)P_i)$$

$$- \frac{1}{2\gamma} \left[\left(\sum_{i=1}^N \mu_i^k b_i \right)^2 \sigma_z^2 + \sum_{i=1}^N (\mu_i^k)^2 (\sigma_\epsilon^2) \right]$$

- ▶ μ_i^k is number of shares purchased by investors in group k for asset i .
- ▶ For agents A and B, under the constraint: $\mu \geq 0$.

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Pricing for “unconstrained” assets

- ▶ For unconstrained assets ($i < \bar{j}$):

$$\begin{cases} (\bar{z} + \lambda)b_i - P_i(1+r) = \frac{1}{\gamma} \left(\left(\sum_{k=1}^N b_k \mu_k^A \right) b_i \sigma_z^2 + \mu_i^A \sigma_\epsilon^2 \right) \\ (\bar{z} - \lambda)b_i - P_i(1+r) = \frac{1}{\gamma} \left(\left(\sum_{k=1}^N b_k \mu_k^B \right) b_i \sigma_z^2 + \mu_i^B \sigma_\epsilon^2 \right) \\ \bar{z}b_i - P_i(1+r) = \frac{1}{\gamma} \left(\left(\sum_{k=1}^N b_k \mu_k^a \right) b_i \sigma_z^2 + \mu_i^a \sigma_\epsilon^2 \right) \end{cases}$$

- ▶ Market clearing condition: $\alpha \left(\frac{1}{2} \mu_i^A + \frac{1}{2} \mu_i^B \right) + (1 - \alpha) \mu_i^a = \frac{1}{N}$
- ▶ Pricing equation similar to CAPM:

$$\underbrace{\bar{z}b_i - P_i(1+r)}_{\text{expected excess return on asset } i} = \frac{1}{\gamma} \underbrace{\left(b_i \sigma_z^2 + \frac{\sigma_\epsilon^2}{N} \right)}_{\text{risk premium}} \quad (*)$$

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- ▶ With first-order condition:

$$\underbrace{\bar{z}b_i - P_i(1+r)}_{\mathbb{E}[\tilde{R}_i]} = \frac{1}{\gamma} \underbrace{\left(b_i \sigma_z^2 + \frac{\sigma_\epsilon^2}{N} \right)}_{\text{risk premium}} - \underbrace{\pi^i}_{\text{speculative premium}} \quad (**)$$

Speculative premium

- ▶ Speculative premium: excess-pricing over no short-sales constraint benchmark ($\alpha = 0$).
- ▶ Derivation: sum FOC and compute $\sum_{k=1}^{\bar{j}-1} b_k \mu_k^B$ using FOC of assets $j < \bar{j}$.
- ▶ Exact form (depends on \bar{j} and $\theta = \frac{\alpha}{1-\frac{\alpha}{2}}$ strictly \nearrow with α):

$$\pi^i = \theta \left(b_i \frac{\sigma_\epsilon^2}{\sigma_\epsilon^2 + \sigma_z^2 \left(\sum_{i < \bar{j}} b_i^2 \right)} \left(\lambda - \frac{\sigma_z^2}{\gamma N} \sum_{k \geq \bar{j}} b_k \right) - \frac{\sigma_\epsilon^2}{\gamma N} \right)$$

- ▶ Speculative premium strictly increases with b_i .

Closing the model: marginal asset

- ▶ Derive equilibrium holdings (conditional on \bar{j}) of pessimists and derive conditions for:
 1. $\frac{\partial U^B}{\partial \mu_{\bar{j}}^B}(\mu^B) < 0$
 2. $\mu_{\bar{j}-1}^B > 0$
- ▶ This is equivalent to:

$$u_{\bar{j}} < \lambda \gamma \leq u_{\bar{j}-1}$$

where (u) is strictly decreasing sequence.

- ▶ We span entire λ space. Unique equilibrium.

Over-pricing

1. Low b assets are priced according to standard CAPM equation.
2. High b assets are over-priced relative to standard CAPM equation. Amount of overpricing increases with λ and α .
 - ▶ More disagreement on high b assets – thus more likely to have pessimists short – thus more over-pricing through short-sale costs. (cost of shorting – idiosyncratic risk – is the same across assets)
 - ▶ High b assets are more disagreement sensitive.
3. $\frac{\partial^2 \text{speculative premium}}{\partial \lambda \partial \alpha} > 0$.
 - ▶ Increasing λ leads to more severe mispricing in high α environment.
4. Cutoff \bar{j} increases with λ .
 - ▶ For high λ , even low b assets can have high disagreement.
5. $\frac{\partial^2 \text{speculative premium}}{\partial \lambda \partial \beta} > 0$: more mispricings when sorted on shorting in high beta stocks

Shorting

There exists $\hat{\lambda} > 0$ such that if $\lambda > \hat{\lambda}$:

1. HFs short at least one asset in equilibrium, i.e. $\mu_N^a < 0$.
2. There exists \tilde{i} such that: $|\mu_N^a| > |\mu_{N-1}^a| \cdots > |\mu_{\tilde{i}}^a| > 0$ and $\forall k < \tilde{i}, \mu_k^a > 0$.
3. $\frac{\partial |\mu_N^a|}{\partial \lambda} > \frac{\partial |\mu_{N-1}^a|}{\partial \lambda} \cdots > \frac{\partial |\mu_{\tilde{i}}^a|}{\partial \lambda} > 0$. A rise in aggregate disagreement leads to a larger increase in shorting for high b assets.

OLG Extension

- ▶ $t = 0, 1, \dots, \infty$
- ▶ Each period t , a new generation of mass 1 is born and invest in the stock market to consume the proceeds at date $t + 1$.
- ▶ A new generation is always composed of 2 groups of agents; arbitrageurs, or Hedge Funds, in proportion $1 - \alpha$, and Mutual funds in proportion α .
- ▶ Investors have mean-variance preferences with risk tolerance parameter 2γ .
- ▶ There are N assets in this economy, whose dividend process each period is given as in our static model by:

$$\tilde{d}^i = b^i \tilde{z} + \tilde{\epsilon}^i$$

OLG Extension

- ▶ Mutual funds born at date t have heterogeneous beliefs about the expected value of \tilde{z}_{t+1} and thus about the expected dividend to be received at date $t + 1$ before reselling the asset.
- ▶ Specifically, there are two groups of mutual funds: group A of optimists MF ($\mathbb{E}^A[\tilde{z}_{t+1}] = \bar{z} + \tilde{\lambda}_t$) and group B of pessimists ($\mathbb{E}^B[\tilde{z}_{t+1}] = \bar{z} - \tilde{\lambda}_t$).
- ▶ $\tilde{\lambda}_t \in \{0, \lambda > 0\}$ is a two-states Markov process with persistence $\rho \in]1/2, 1[$.

OLG Extension

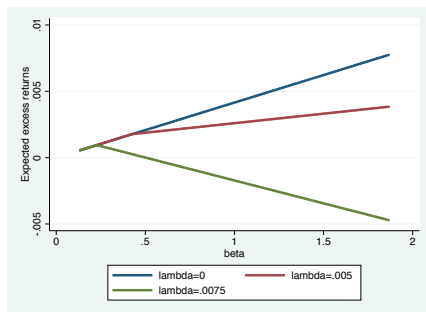
1. When ρ is large, same basic results from static setting.
2. Plus share turnover: high beta stocks have higher turnover due to more shorting and more shares which are then traded when generations changeover.
3. The differential turnover between high w assets ($j \geq \hat{i}$) and low w assets ($j < \hat{i}$) is strictly greater for high disagreement states ($\tilde{\lambda} = \lambda > 0$) than for low disagreement states ($\tilde{\lambda} = 0$).

Resale Option and Bubble

- ▶ Suppose $\tilde{\lambda}_t = 0$.
- ▶ Potential disagreement at $t + 1$ leads to potential binding constraints when $\lambda > 0$.
- ▶ Current generation of traders anticipate that resale price will be high when short-sales constraints are binding in the $\lambda > 0$ state.
- ▶ This is a version of the resale option of Harrison and Kreps 1978 and Scheinkman and Xiong 2003 (except each generation has to sell).
- ▶ Bubble accompanied by high turnover due to shorting by hedge funds.
- ▶ Like classic theories of bubbles with over-trading (too much demand met by arbs shorting)

Illustration: SML Slope Conditional on Disagreement

- Parameters: $N = 100$, $\sigma_z^2 = .0022$, $\sigma_\epsilon^2 = .029$, $\alpha = .63$, $\gamma = .6$, $\rho = 0.94$.



When Some Investors Head for the Exit (w/ Wenxi Jiang)

- ▶ Chen-Hong-Stein: Decrease in breadth of mutual fund ownership (change in fraction of MF owners = entry rate - exit rate) forecasts low stock returns
- ▶ Asquith-Pathak-Ritter: Top short-interest ratio (shares shorted to shares outstanding) decile under-performs rest of the stocks
- ▶ Show exit rate better captures short-sales constraints. Entry rate might reflect changes in limited participation and higher prices and more shorting
- ▶ A new measure of hedge fund breadth and exit rate which work better than mutual fund breadth.
- ▶ These all work better in high beta stocks, consistent with $\frac{\partial^2 \text{speculative premium}}{\partial \lambda \partial \beta} > 0$.

Short Interest Forecast of Quarterly Returns

| <i>1991 to 2008</i> | | Sort on short interest ratio | | | | | | | | | |
|-----------------------|---------|-------------------------------------|---------|---------|---------|---------|--------------|---------|---------|---------|--|
| <i>Equal-Weighted</i> | | Raw Return | | | | | DGTW Returns | | | | |
| | Lo Beta | Q2 | Q3 | Q4 | Hi Beta | Lo Beta | Q2 | Q3 | Q4 | Hi Beta | |
| Bottom 50% | 2.73% | 2.72% | 3.43% | 2.55% | 1.84% | 0.32% | 0.32% | 0.88% | 0.50% | 0.08% | |
| | (3.22) | (2.93) | (3.28) | (2.00) | (1.05) | (0.74) | (0.90) | (2.89) | (2.09) | (0.14) | |
| Top 5% | 1.45% | 2.01% | 1.47% | 0.17% | -0.42% | -0.65% | -0.01% | -0.38% | -1.65% | -2.95% | |
| | (0.89) | (1.29) | (0.93) | (0.10) | (-0.17) | (-0.49) | (-0.01) | (-0.37) | (-2.16) | (-2.47) | |
| Hi - Lo | -1.28% | -0.72% | -1.96% | -2.38% | -2.26% | -0.97% | -0.33% | -1.26% | -2.15% | -3.03% | |
| | (-0.94) | (-0.68) | (-1.84) | (-2.49) | (-2.26) | (-0.74) | (-0.39) | (-1.19) | (-2.56) | (-2.99) | |

Among high beta stocks, in high disagreement periods (top 30%), Hi-Lo is -2.17% per quarter RAW. In low disagreement periods (bottom 30%) only -1.43% RAW.

Hedge Fund Exit Rate Forecast of Quarterly Returns

| 1991 to 2008 Equal-Weighted | Sort on HF EXIT | | | | | | | | | |
|--------------------------------|-----------------|---------|--------|---------|---------|--------------|---------|--------|---------|---------|
| | Raw Return | | | | | DGTW Returns | | | | |
| | Lo Beta | Q2 | Q3 | Q4 | Hi Beta | Lo Beta | Q2 | Q3 | Q4 | Hi Beta |
| Bottom 50% | 2.68% | 2.76% | 3.09% | 2.53% | 1.93% | 0.29% | 0.27% | 0.61% | 0.45% | -0.25% |
| | (3.21) | (2.88) | (2.98) | (1.95) | (0.94) | (0.68) | (0.84) | (2.64) | (1.66) | (-0.33) |
| Top 5% | 4.00% | 2.10% | 3.36% | 0.78% | -0.63% | 2.03% | -0.58% | 1.26% | -1.54% | -3.08% |
| | (4.20) | (2.19) | (2.54) | (0.41) | (-0.31) | (2.65) | (-1.00) | (1.06) | (-1.37) | (-3.02) |
| Hi - Lo | 1.35% | -0.45% | 0.53% | -1.65% | -2.44% | 1.71% | -0.75% | 0.72% | -2.01% | -2.57% |
| | (2.85) | (-0.86) | (0.62) | (-1.58) | (-2.69) | (2.94) | (-1.45) | (0.66) | (-1.92) | (-2.56) |

Among high beta stocks, in uncertain periods, Hi-Lo is -3.24% RAW. It is -2.12% RAW.

Mutual Fund Exit Rate Forecasts Quarterly Returns

| 1981 to 2008 Equal-Weighted | Raw Return | | | | | Sort on EF EXIT DGTW Returns | | | | |
|--------------------------------|------------|---------|---------|---------|---------|---------------------------------|---------|---------|---------|---------|
| | Lo Beta | Q2 | Q3 | Q4 | Hi Beta | Lo Beta | Q2 | Q3 | Q4 | Hi Beta |
| Bottom 50% | 3.06% | 3.49% | 3.54% | 3.01% | 2.19% | 0.12% | 0.43% | 0.49% | 0.20% | -0.48% |
| | (4.66) | (4.48) | (4.01) | (2.87) | (1.49) | (0.35) | (1.85) | (2.62) | (0.94) | (-0.86) |
| Top 5% | 3.04% | 2.77% | 2.57% | 1.77% | -0.08% | -0.14% | -0.34% | 0.43% | -0.56% | -2.36% |
| | (3.04) | (2.57) | (2.38) | (1.40) | (-0.05) | (-0.18) | (-0.39) | (0.81) | (-0.88) | (-3.19) |
| Hi - Lo | -0.02% | -0.72% | -0.97% | -1.24% | -2.26% | -0.26% | -0.76% | -0.06% | -0.76% | -1.88% |
| | (-0.03) | (-1.02) | (-1.56) | (-2.11) | (-3.53) | (-0.37) | (-0.98) | (-0.12) | (-1.25) | (-2.61) |

Among high beta stocks, in high uncertainty periods, Hi-Lo is -2.76%. It is -2.58% in low uncertainty periods.

Conclusion

- ▶ Bridge of Behavioral Finance to CAPM
- ▶ Behavioral Beta Finance or Behavioral Macro-Finance
 - ▶ Speculative investors like beta \Rightarrow high beta assets command high prices.
 - ▶ High volatility assets associated with higher expected returns.
- ▶ Many potential links of existing work back to the cross-section and beta, including capital budgeting implications.